FIITJEE Solutions to JEE(Main)-2015

PAPER – 1 CHEMSITRY, MATHEMATICS & PHYSICS

Test Booklet Code

B

Important Instructions:

- 1. The test is of **3 hours** duration.
- 2. The Test Booklet consists of **90** questions. The maximum marks are 360.
- 3. There are *three* parts in the question paper A, B, C consisting of **Chemistry**, **Mathematics and Physics** having 30 questions in each part of equal weightage. Each question is allotted **4 (four)** marks for each correct response.
- 4. Candidates will be awarded marks as started above in instruction No. 3 for correct response of each question. 1/4(one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 5. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 4 above.

PART A - CHEMISTRY

- *1. Which of the following is the energy of a possible excited state of hydrogen?
 - (1) -6.8 eV

(2) -3.4 eV

(3) +6.8 eV

(4) +13.6 eV

2. In the following sequence of reactions:

Toluene $\xrightarrow{\text{KMnO}_4}$ A $\xrightarrow{\text{SOCl}_2}$ B $\xrightarrow{\text{H}_2/\text{Pd}}$ C,

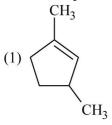
The product C is:

(1) $C_6H_5CH_3$

(2) $C_6H_5CH_2OH$

(3) C_6H_5CHO

- (4) C₆H₅COOH
- *3. Which compound would give 5-keto-2-methyl hexanal upon ozonolysis?



(2) CH₃

(3)
$$H_3C$$

- (4) CH₃ CH₃
- *4. The ionic radii (in Å) of N^{3-} , O^{2-} and F^{-} are respectively:
 - (1) 1.36, 1.71 and 1.40

(2) 1.71, 1.40 and 1.36

(3) 1.71, 1.36 and 1.40

(4) 1.36, 1.40 and 1.71

- 5. The color of $KMnO_4$ is due to:
 - (1) d d transition

(2) $L \rightarrow M$ charge transfer transition

(3) $\sigma - \sigma^*$ transition

- (4) $M \rightarrow L$ charge transfer transition
- 6. **Assertion :** Nitrogen and Oxygen are the main components in the atmosphere but these do not react to form oxides of nitrogen.

Reason: The reaction between nitrogen and oxygen requires high temperature.

- (1) Both assertion and reason are correct, but the reason is not the correct explanation for the assertion
- (2) The assertion is incorrect, but the reason is correct
- (3) Both the assertion and reason are incorrect
- (4) Both assertion and reason are correct, and the reason is the correct explanation for the assertion
- 7. Which of the following compounds is not an antacid?
 - (1) Cimetidine

(2) Phenelzine

(3) Ranitidine

- (4) Aluminium hydroxide
- 8. In the context of the Hall-Heroult process for the extraction of Al, which of the following statements is false?
 - (1) Al₂O₃ is mixed with CaF₂ which lowers the melting point of the mixture and brings conductivity
 - (2) Al³⁺ is reduced at the cathode to form Al
 - (3) Na₃AlF₆ serves as the electrolyte
 - (4) CO and CO₂ are produced in this process

9. Match the catalysts to the correct processes:

Catalyst

Process

(A) TiCl₃ (i) Wacker process

PdCl₂ (B)

Ziegler – Natta polymerization (ii)

(C) CuCl₂

Contact process (iii)

(D) V_2O_5

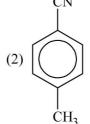
- Deacon's process (iv)
- (1) (A) (ii), (B) (i), (C) (iv), (D) (iii)
- (3) (A) (iii), (B) (i), (C) (ii), (D) (iv)
- (2) (A) (ii), (B) (iii), (C) (iv), (D) (i)(4) (A) - (iii), (B) - (ii), (C) - (iv), (D) - (i)

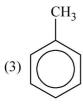
10. In the reaction:

$$\begin{array}{c|c}
 & \text{NH}_2 \\
\hline
 & \text{NaNO}_2/\text{HCI} \\
\hline
 & \text{O-5°C}
\end{array} \rightarrow D \xrightarrow{\text{Cucn/KCN}} E + N_2$$

$$\begin{array}{c}
 & \text{CH}_3
\end{array}$$

the product E is





- COOH CH₃
- 11. Which polymer is used in the manufacture of paints and lacquers?
 - (1) Glyptal

(2) Polypropene

(3) Poly vinyl chloride

- (4) Bakelite
- 12. The number of geometric isomers that can exist for square planar [Pt (Cl) (py) (NH₃) (NH₂OH)]⁺ is (py = pyridine):
 - (1) 3

(2) 4

(3) 6

- (4) 2
- Higher order (>3) reactions are rare due to: 13.
 - (1) increase in entropy and activation energy as more molecules are involved
 - (2) shifting of equilibrium towards reactants due to elastic collisions
 - (3) loss of active species on collision
 - (4) low probability of simultaneous collision of all the reacting species
- 14. Which among the following is the most reactive?
 - (1) Br₂

(2) I_2

(3) IC1

(4) Cl₂

15.	Two Faraday of electricity is passed through a solutathode is: (at. mass of Cu = 63.5 amu) (1) 63.5 g (3) 127 g	(2)	of $CuSO_4$. The mass of copper deposited at the $\begin{array}{c} 2\ g\\ 0\ g \end{array}$		
*16.	3 g of activated charcoal was added to 50 mL of acet filtered and the strength of the filtrate was found to gram of charcoal) is:	be (0.042 N. The amount of acetic acid adsorbed (per		
	(1) 36 mg (3) 54 mg		42 mg 18 mg		
17.	The synthesis of alkyl fluorides is best accomplished (1) Sandmeyer's reaction (3) Swarts reaction	(2)	Finkelstein reaction Free radical fluorination		
*18.	The molecular formula of a commercial resin $C_8H_7SO_3Na(Mol. Wt. 206)$. What would be the max in mole per gram resin?	imun	n uptake of $Ca^{\frac{3}{2}}$ ions by the resin when expressed		
	(1) $\frac{1}{206}$	(2)	$\frac{2}{309}$		
	(3) $\frac{1}{412}$	(4)	$\frac{2}{309}$ $\frac{1}{103}$		
19.	Which of the vitamins given below is water soluble? (1) Vitamin D	(2)	Vitamin E		
	(3) Vitamin K	` /	Vitamin C		
*20.	The intermolecular interaction that is dependent on the inverse cube of distance between the molecule is:				
	(1) ion-dipole interaction(3) hydrogen bond	, ,	London force ion-ion interaction		
*21.	The following reaction is performed at 298 K.				
	$2NO(g) + O_2(g) \Longrightarrow 2NO_2(g)$				
	The standard free energy of formation of NO(g) is 86.6 kJ/mol at 298 K. What is the standard free energy of formation of NO ₂ (g) at 298 K? ($K_P = 1.6 \times 10^{12}$)				
	(1) $86600 + R(298) \ln(1.6 \times 10^{12})$	(2)	$86600 - \frac{\ln(1.6 \times 10^{12})}{R(298)}$		
	(3) $0.5[2\times86,600 - R(298) \ln(1.6\times10^{12})]$		$R(298)\ln(1.6\times10^{12}) - 86600$		
22.	Which of the following compounds is not colored ye	llow	?		
	(1) $K_3[Co(NO_2)_6]$		$(NH_4)_3[As(Mo_3O_{10})_4]$		
	(3) BaCrO ₄	(4)	$Zn_2[Fe(CN)_6]$		
*23.	In Carius method of estimation of halogens, 250 mg percentage of bromine in the compound is: (at. Mass (1) 36		= 108; Br = 80)		
	(3) 60	(4)			
24.	Sodium metal crystallizes in a body centred cubic sodium atom is approximately:	lattic	be with a unit cell edge of 4.29Å . The radius of		
	(1) 3.22 Å	(2)	5.72 Å		
	(3) 0.93 Å	(4)	$1.86\mathrm{\AA}$		

*25.	Which of the following compounds will exhibit geom (1) 3-Phenyl-1-butene (3) 1,1-Diphenyl-1-propane	netrical isomerism? (2) 2-Phenyl-1-butene (4) 1-Phenyl-2-butene
26.	The vapour pressure of acetone at 20°C is 185 torr. V 100 g of acetone at 20°C, its vapour pressure was 18: (1) 64 (3) 488	When 1.2 g of a non-volatile substance was dissolved in 3 torr. The molar mass (g mol ⁻¹) of the substance is: (2) 128 (4) 32
*27.	From the following statements regarding H ₂ O ₂ , choo (1) It decomposes on exposure to light (2) It has to be stored in plastic or wax lined glass b (3) It has to be kept away from dust (4) It can act only as an oxidizing agent	
*28.	Which one of the following alkaline earth metal sulpenthalpy? (1) BeSO ₄ (3) SrSO ₄	chates has its hydration enthalpy greater than its lattice (2) BaSO ₄ (4) CaSO ₄
*29.	The standard Gibbs energy change at 300 K for the the composition of the reaction mixture is $[A] = \frac{1}{2}$, $[R = 8.314 \text{ J/K/mol}, e = 2.718]$ (1) reverse direction because $Q > K_c$ (2) forward direction because $Q < K_c$ (3) reverse direction because $Q < K_c$ (4) forward direction because $Q > K_c$	reaction $2A \Longrightarrow B + C$ is 2494.2 J. At a given time, $B = 2$ and $C = \frac{1}{2}$. The reaction proceeds in the:
30.	Which one has the highest boiling point? (1) Ne (3) Xe	(2) Kr (4) He

PART B – MATHEMATICS

*31.	The sum of coefficients of integral powers of x in the binomial expansion of $(1-2\sqrt{x})^{50}$ is:				
	$(1) \frac{1}{2} (3^{50})$	$(2) \ \frac{1}{2} (3^{50} - 1)$			
	$(3) \ \frac{1}{2} \Big(2^{50} + 1 \Big)$	$(4) \ \frac{1}{2} \Big(3^{50} + 1 \Big)$			
32.	Let $f(x)$ be a polynomial of degree four having extreme values at $x = 1$ and $x = 2$. If $\lim_{x \to 0} \left[1 + \frac{1}{x} \right]$				
	then f(2) is equal to:				
	(1) - 4	(2) 0			
	(3) 4	(4) - 8			
*33.	tions is 16. If one of the observation valued 16 is deleted dded to the data, then the mean of the resultant data, is:				
	(1) 16.0 (3) 14.0	(2) 15.8 (4) 16.8			
*34.	The sum of first 9 terms of the series $\frac{1^3}{1} + \frac{1^3 + 2^3}{1+3} + \frac{1}{1+3}$	$\frac{1^3 + 2^3 + 3^3}{1 + 3 + 5} + \dots is:$			
	(1) 96	(2) 142			
	(3) 192	(4) 71			
*35. Let O be the vertex and Q be any point on the parabola, $x^2 = 8y$. If the point P divides the li internally in the ratio 1:3, then the locus of P is:					
	(1) $y^2 = x$	(2) $y^2 = 2x$ (4) $x^2 = y$			
	$(3) x^2 = 2y$	$(4) x^2 = y$			
*36.	Let α and β be the roots of equation $x^2 - 6x - 2 = 0$. If $a_n = \alpha^n - \beta^n$, for $n \ge 1$, then the value of $\frac{a_{10} - 2a_8}{2a_9}$ is				
	equal to:	,			
	(1) - 6	(2) 3			
	(3) - 3	(4) 6			
37.	If 12 identical balls are to be placed in 3 identical be exactly 3 balls is:	poxes, then the probability that one of the boxes contains			
	(1) $55\left(\frac{2}{3}\right)^{10}$	(2) $220\left(\frac{1}{3}\right)^{12}$			
	(1) 33 $(\overline{3})$	$(2) 220 \left(\frac{1}{3}\right)$			
	(3) $22\left(\frac{1}{3}\right)^{11}$	$(4) \frac{55}{3} \left(\frac{2}{3}\right)^{11}$			
*38.	A complex number z is said to be unimodular if z	$ z = 1$. Suppose z_1 and z_2 are complex numbers such that			
	$\frac{z_1 - 2z_2}{2 - z_1\overline{z}_2}$ is unimodular and z_2 is not unimodular. T	Then the point z_1 lies on a:			
	$\mathcal{L} - \mathbf{Z}_1 \mathbf{Z}_2$				

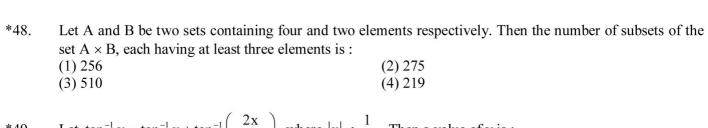
(2) circle of radius 2.

(4) straight line parallel to x-axis.

(1) straight line parallel to y-axis.

(3) circle of radius $\sqrt{2}$.

39.	The integral $\int \frac{dx}{x^2(x^4+1)^{3/4}}$ equals:				
	$(1) (x^4 + 1)^{1/4} + c$	$(2) - (x^4 + 1)^{1/4} + c$			
	$(3) - \left(\frac{x^4 + 1}{x^4}\right)^{1/4} + c$	$(4) \left(\frac{x^4 + 1}{x^4}\right)^{1/4} + c$			
*40.	The number of points, having both co-ordinates a vertices $(0, 0)$, $(0, 41)$ and $(41, 0)$, is:	as integers, that lie in the interior of the triangle with			
	(1) 861 (3) 780	(2) 820 (4) 901			
41.		of intersection of the line $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$ and the			
	plane $x - y + z = 16$, is:				
	(1) 8	(2) $3\sqrt{21}$			
	(3) 13	(4) $2\sqrt{14}$			
42.	The equation of the plane containing the line $2x - 3y + 6z = 1$, is:	5y + z = 3; $x + y + 4z = 5$, and parallel to the plane, $x + 4z = 3$			
	(1) x + 3y + 6z = -7	(2) x + 3y + 6z = 7			
	(3) 2x + 6y + 12z = -13	(4) 2x + 6y + 12z = 13			
43.		The area (in sq. units) of the region described by $\{(x, y) : y^2 \le 2x \text{ and } y \ge 4x - 1\}$ is:			
	$(1) \frac{5}{64}$	$(2) \frac{15}{64}$			
	$(3) \frac{9}{32}$	$(4) \frac{7}{32}$			
*44.	If m is the A.M. of two distinct real numbers ℓ a means between ℓ and n, then $G_1^4 + 2G_2^4 + G_3^4$ equal	nd n (ℓ , n > 1) and G_1 , G_2 and G_3 are three geometric is :			
	$(1) 4\ell m^2 n$	(2) $4\ell \text{mn}^2$			
	$(3) 4\ell^2 m^2 n^2$	(4) $4\ell^2$ mn			
*45.	Locus of the image of the point (2, 3) in the line (2x	$(x-3y+4) + k(x-2y+3) = 0, k \in \mathbb{R}$, is a:			
	(1) straight line parallel to y-axis.	(2) circle of radius $\sqrt{2}$.			
	(3) circle of radius $\sqrt{3}$.	(4) straight line parallel to x-axis.			
*46.	The area (in sq. units) of the quadrilateral formed by the tangents at the end points of the latera recta to the $x^2 - y^2$				
	ellipse $\frac{x^2}{9} + \frac{y^2}{5} = 1$, is:				
	(1) 18	(2) $\frac{27}{2}$ (4) $\frac{27}{4}$			
	(3) 27	$(4) \frac{27}{4}$			
*47.	The number of integers greater than 6,000 that ca repetition, is:	n be formed, using the digits 3, 5, 6, 7 and 8, without			
	(1) 192	(2) 120			
	(3) 72	(4) 216			



*49. Let
$$\tan^{-1} y = \tan^{-1} x + \tan^{-1} \left(\frac{2x}{1 - x^2} \right)$$
, where $|x| < \frac{1}{\sqrt{3}}$. Then a value of y is:

(1) $\frac{3x + x^3}{1 - 3x^2}$
(2) $\frac{3x - x^3}{1 + 3x^2}$
(3) $\frac{3x + x^3}{1 + 3x^2}$

50. The integral
$$\int_{2}^{4} \frac{\log x^2}{\log x^2 + \log(36 - 12x + x^2)} dx$$
 is equal to:

- (1) 4 (3) 6 (2) 1 (4) 2
- *51. The negation of $\sim s \lor (\sim r \land s)$ is equivalent to : $(1) s \land (r \land \sim s) \qquad (2) s \lor (r \lor \sim s)$ $(3) s \land r \qquad (4) s \land \sim r$
- *52. If the angles of elevation of the top of a tower from three collinear points A, B and C, on a line leading to the foot of the tower, are 30°, 45° and 60° respectively, then the ratio, AB : BC, is :

 (1) $\sqrt{3}$: $\sqrt{2}$ (2) 1: $\sqrt{3}$
 - (1) $\sqrt{3}:\sqrt{2}$ (2) 1: $\sqrt{3}$ (3) 2: 3 (4) $\sqrt{3}:1$
- 53. $\lim_{x \to 0} \frac{(1 \cos 2x)(3 + \cos x)}{x \tan 4x}$ is equal to:
 (1) 3 (2) 2
 (3) $\frac{1}{2}$ (4) 4
- 54. Let \vec{a} , \vec{b} and \vec{c} be three non-zero vectors such that no two of them are collinear and $(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$.

 If θ is the angle between vectors \vec{b} and \vec{c} , then a value of $\sin \theta$ is:
 - (1) $\frac{-\sqrt{2}}{3}$ (2) $\frac{2}{3}$ (3) $\frac{-2\sqrt{3}}{3}$ (4) $\frac{2\sqrt{2}}{3}$
- 55. If $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{bmatrix}$ is a matrix satisfying the equation $AA^{T} = 9I$, where I is 3×3 identity matrix, then

ordered pair (a, b) is equal to:

$$\begin{array}{c} (1) (-2, 1) \\ (3) (-2, -1) \end{array}$$

$$\begin{array}{c} (2) (2, 1) \\ (4) (2, -1) \end{array}$$

56.	If the function. $g(x) = \begin{cases} k\sqrt{x+1}, & 0 \le x \le 3 \\ mx+2, & 3 < x \le 5 \end{cases}$ is diff	Perentiable, then the value of $k + m$ is:
	$(1) \frac{16}{5}$	(2) $\frac{10}{3}$
	(3) 4	(4) 2
57.	The set of all values of λ for which the system of lin $2x_1 - 2x_2 + x_3 = \lambda x_1$ $2x_1 - 3x_2 + 2x_3 = \lambda x_2$ $-x_1 + 2x_2 = \lambda x_3$ has a non-trivial solution,	ear equations :
	(1) is a singleton.	(2) contains two elements.
	(3) contains more than two elements.	(4) is an empty set.
*58.	The normal to the curve, $x^2 + 2xy - 3y^2 = 0$, at (1, 1) (1) meets the curve again in the second quadrant. (2) meets the curve again in the third quadrant. (3) meets the curve again in the fourth quadrant. (4) does not meet the curve again.):
*59.	The number of common tangents to the circles x^2 + is:	$y^2 - 4x - 6y - 12 = 0$ and $x^2 + y^2 + 6x + 18y + 26 = 0$,
	(1) 2	(2) 3
	(3) 4	(4) 1

Let y(x) be the solution of the differential equation $(x \log x) \frac{dy}{dx} + y = 2x \log x, (x \ge 1)$. Then y(e) is equal

(2) 2 (4) e

60.

to:
(1) 0

(3) 2e

PART C - PHYSICS

- 61. As an electron makes a transition from an excited state to the ground state of a hydrogen like atom/ion:
 - (1) kinetic energy, potential energy and total energy decrease
 - (2) kinetic energy decreases, potential energy increases but total energy remains same
 - (3) kinetic energy and total energy decrease but potential energy increases
 - (4) its kinetic energy increases but potential energy and total energy decrease
- *62. The period of oscillation of a simple pendulum is $T = 2\pi \sqrt{\frac{L}{g}}$. Measured value of L is 20.0 cm known to 1

mm accuracy and time for 100 oscillations of the pendulum is found to be 90 s using wrist watch of 1 s resolution. The accuracy in the determination of g is:

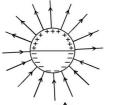
(1) 3%

(2) 1%

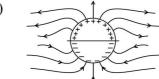
(3) 5%

- (4) 2%
- 63. A long cylindrical shell carries positive surface charge σ in the upper half and negative surface charge $-\sigma$ in the lower half. The electric field lines around the cylinder will look like figure given in: (figures are schematic and not drawn to scale)

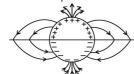




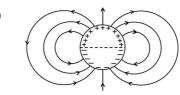
(2)



(3)



(4)



- 64. A signal of 5 kHz frequency is amplitude modulated on a carrier wave of frequency 2 MHz. The frequencies of the resultant signal is/are:
 - (1) 2005 kHz, and 1995 kHz

(2) 2005 kHz, 2000 kHz and 1995 kHz

(3) 2000 kHz and 1995 kHz

- (4) 2 MHz only
- *65. Consider a spherical shell of radius R at temperature T. The black body radiation inside it can be considered as an ideal gas of photons with internal energy per unit volume $u = \frac{U}{V} \propto T^4$ and pressure

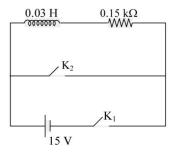
 $p = \frac{1}{3} \left(\frac{U}{V} \right)$. If the shell now undergoes an adiabatic expansion the relation between T and R is:

(1) $T \propto e^{-3R}$

(2) $T \propto \frac{1}{R}$

(3) $T \propto \frac{1}{R^3}$

- (4) $T \propto e^{-R}$
- An inductor (L = 0.03 H) and a resistor (R = 0.15 kΩ) are connected in series to a battery of 15V EMF in a circuit shown. The key K_1 has been kept closed for a long time. Then at t = 0, K_1 is opened and key K_2 is closed simultaneously. At t = 1 ms, the current in the circuit will be: ($e^5 \cong 150$)
 - (1) 67 mA
 - (2) 6.7 mA
 - (3) 0.67 mA
 - (4) 100 mA



*67. A pendulum made of a uniform wire of cross sectional area A has time period T. When an additional mass M is added to its bob, the time period changes to T_M. If the Young's modulus of the material of the wire is

Y then $\frac{1}{Y}$ is equal to: $(g = gravitational\ acceleration)$

$$(1)\left[\left(\frac{T_{M}}{T}\right)^{2}-1\right]\frac{Mg}{A}$$

$$(2) \left[1 - \left(\frac{T_{M}}{T} \right)^{2} \right] \frac{A}{Mg}$$

$$(3) \left[1 - \left(\frac{T}{T_{M}} \right)^{2} \right] \frac{A}{Mg}$$

$$(4) \left[\left(\frac{T_{M}}{T} \right)^{2} - 1 \right] \frac{A}{Mg}$$

- 68. A red LED emits light at 0.1 watt uniformly around it. The amplitude of the electric field of the light at a distance of 1 m from the diode is:
 - (1) 2.45 V/m

(2) 5.48 V/m

(3) 7.75 V/m

- (4) 1.73 V/m
- Two coaxial solenoids of different radii carry current I in the same direction. Let \vec{F}_1 be the magnetic force on the inner solenoid due to the outer one and \vec{F}_2 be the magnetic force on the outer solenoid due to the inner one. Then:
 - (1) \vec{F}_1 is radially inwards and \vec{F}_2 is radially outwards
 - (2) \vec{F}_1 is radially inwards and $\vec{F}_2 = 0$
 - (3) \vec{F}_1 is radially outwards and $\vec{F}_2 = 0$
 - (4) $\vec{F}_1 = \vec{F}_2 = 0$
- *70. Consider an ideal gas confined in an isolated closed chamber. As the gas undergoes an adiabatic expansion the average time of collision between molecules increases as V^q , where V is the volume of the gas. The value of q is :

$$\left(\gamma = \frac{C_p}{C_v}\right)$$

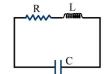
 $(1) \frac{3\gamma - 5}{6}$

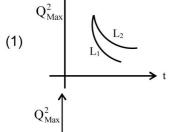
(2) $\frac{\gamma+1}{2}$

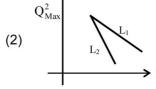
 $(3) \frac{\gamma - 1}{2}$

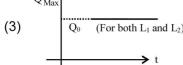
- $(2) \frac{3\gamma + 5}{6}$
- 71. An LCR circuit is equivalent to a damped pendulum. In an LCR circuit the capacitor is charged to Q_0 and then connected to the L and R as shown.

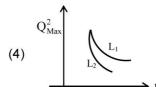
If a student plots graphs of the square of maximum charge ($Q_{_{Max}}^2$) on the capacitor with time (t) for two different values L_1 and L_2 ($L_1 > L_2$) of L then which of the following represents this graph correctly? (Plots are schematic and not drawn to scale)









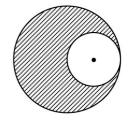


*72. From a solid sphere of mass M and radius R, a spherical portion of radius R/2 is removed, as shown in the figure. Taking gravitational potential V = 0 at $r = \infty$, the potential at the centre of the cavity thus formed is (G = gravitational constant)



 $(2) - \frac{2GM}{3R}$ $(4) \frac{-GM}{2R}$

$$(3) - \frac{2GM}{R}$$



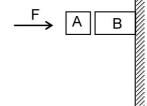
A train is moving on a straight track with speed 20 ms⁻¹. It is blowing its whistle at the frequency of 1000 *73. Hz. The percentage change in the frequency heard by a person standing near the track as the train passes him is (speed of sound = 320 ms⁻¹) close to :

(1) 12 %

(2) 18 %

(4) 6 %

*74. Given in the figure are two blocks A and B of weight 20 N and 100 N respectively. These are being pressed against a wall by a force F as shown. If the coefficient of friction between the blocks is 0.1 and between block B and the wall is 0.15, the frictional force applied by the wall on block B is



(1) 80 N

(2) 120 N

(3) 150 N

(4) 100 N

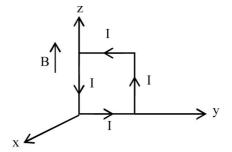
*75. Distance of the centre of mass of a solid uniform cone from its vertex is z_0 . If the radius of its base is R and its height is h then z_0 is equal to :

(3)
$$\frac{3h^2}{8R}$$

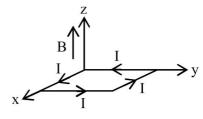
(2) $\frac{5h}{8}$ (4) $\frac{h^2}{4R}$

A rectangular loop of sides 10 cm and 5 cm carrying a current I of 12 A is placed in different orientations 76. as shown in the figures below:

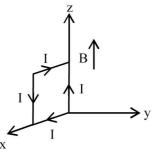
(a)



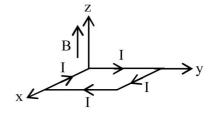
(b)



(c)



(d)



If there is a uniform magnetic field of 0.3 T in the positive z direction, in which orientations the loop would be in (i) stable equilibrium and (ii) unstable equilibrium?

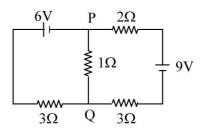
(1) (a) and (c), respectively

(2) (b) and (d), respectively

(3) (b) and (c), respectively

(4) (a) and (b), respectively

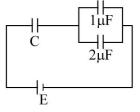
- 77. In the circuit shown, the current in the 1Ω resistor is :
 - (1) 0 A
 - (2) 0.13 A, from Q to P
 - (3) 0.13 A, from P to Q
 - (4) 1.3 A, from P to Q



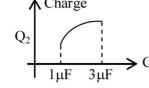
- A uniformly charged solid sphere of radius R has potential V_0 (measured with respect to ∞) on its surface. For this sphere the equipotential surfaces with potentials $\frac{3V_0}{2}, \frac{5V_0}{4}, \frac{3V_0}{4}$ and $\frac{V_0}{4}$ have radius R_1, R_2, R_3 and R_4 respectively. Then
 - (1) $R_1 \neq 0$ and $(R_2 R_1) > (R_4 R_3)$
- (2) $R_1 = 0$ and $R_2 < (R_4 R_3)$

(3) $2R < R_4$

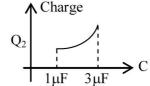
- (4) $R_1 = 0$ and $R_2 > (R_4 R_3)$
- 79. In the given circuit, charge Q_2 on the $2\mu F$ capacitor changes as C is varied from $1\mu F$ to $3\mu F$. Q_2 as a function of 'C' is given properly by : *(figures are drawn schematically and are not to scale)*



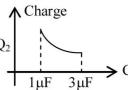
(1)



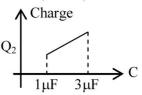
(2)



(3)



(4)

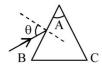


- *80. A particle of mass m moving in the x direction with speed 2v is hit by another particle of mass 2m moving in the y direction with speed v. If the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to
 - (1) 50%

(2) 56%

(3) 62%

- (4) 44%
- 81. Monochromatic light is incident on a glass prism of angle A. If the refractive index of the material of the prism is μ , a ray, incident at an angle θ , on the face AB would get transmitted through the face AC of the prism provided:



- (1) $\theta < \sin^{-1} \left[\mu \sin \left(A \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$
- (2) $\theta > \cos^{-1} \left[\mu \sin \left(A + \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$
- (3) $\theta < \cos^{-1} \left[\mu \sin \left(A + \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$
- (4) $\theta > \sin^{-1} \left[\mu \sin \left(A \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$
- *82. From a solid sphere of mass M and radius R a cube of maximum possible volume is cut. Moment of inertia of cube about an axis passing through its center and perpendicular to one of its faces is:
 - $(1) \frac{MR^2}{16\sqrt{2}\pi}$

(2) $\frac{4MR^2}{9\sqrt{3}\pi}$

(3) $\frac{4MR^2}{3\sqrt{3}\pi}$

(4) $\frac{MR^2}{32\sqrt{2}\pi}$

List – I			List – II		
(A)	Franck-Hertz Experiment	(i)	Particle nature of light		
(B)	Photo-electric experiment	(ii)	Discrete energy levels of atom		
(C)	Davison – Germer Experiment	(iii)	Wave nature of electron		
		(iv)	Structure of atom		

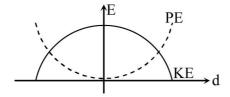
- (1) (A) (ii) (B) -
 - (B) (iv) (C) (iii)
- (2) (A) (ii)(3) (A) - (iy)
- (B)-(i) (C)-(iii)
- (3) (A) (iv)(4) (A) - (i)
- (B)-(iii) (C)-(ii)
- $(B) (iv) \qquad (C) (iii)$
- When 5V potential difference is applied across a wire of length 0.1 m, the drift speed of electrons is $2.5 \times 10^{-4} \text{ ms}^{-1}$. If the electron density in the wire is $8 \times 10^{28} \text{ m}^{-3}$, the resistivity of the material is close to:
 - (1) $1.6 \times 10^{-7} \,\Omega \text{m}$

(2) $1.6 \times 10^{-6} \,\Omega \text{m}$

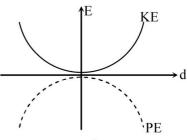
(3) $1.6 \times 10^{-5} \Omega \text{m}$

- (4) $1.6 \times 10^{-8} \,\Omega \text{m}$
- *85. For a simple pendulum, a graph is plotted between its kinetic energy (KE) and potential energy (PE) against its displacement d. Which one of the following represents these correctly? (Graphs are schematic and not drawn to scale)

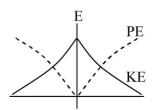
(1)



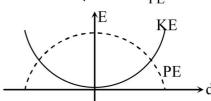
(2)



(3)

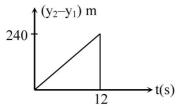


(4)

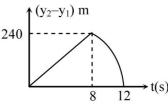


- *86. Two stones are thrown up simultaneously from the edge of a cliff 240 m high with initial speed of 10 m/s and 40 m/s respectively. Which of the following graph best represents the time variation of relative position of the second stone with respect to the first?
 - (Assume stones do not rebound after hitting the ground and neglect air resistance, take $g = 10 \text{ m/s}^2$) (The figures are schematic and not drawn to scale)

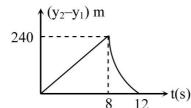
(1)



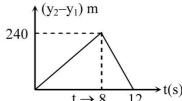
(2)



(3)



(4)



- *87. A solid body of constant heat capacity 1 J/°C is being heated by keeping it in contact with reservoirs in two ways:
 - (i) Sequentially keeping in contact with 2 reservoirs such that each reservoir supplies same amount of heat.
 - (ii) Sequentially keeping in contact with 8 reservoirs such that each reservoir supplies same amount of heat. In both the cases body is brought from initial temperature 100°C to final temperature 200°C. Entropy change of the body in the two cases respectively is:
 - (1) ln2, ln2

(2) ln2, 2ln2

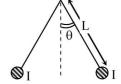
(3) 2ln2, 8ln2

- (4) ln2, 4ln2
- 88. Assuming human pupil to have a radius of 0.25 cm and a comfortable viewing distance of 25 cm, the minimum separation between two objects that human eye can resolve at 500 nm wavelength is:
 - (1) $30 \mu m$

(2) $100 \mu m$

(3) 300 µm

- (4) $1 \mu m$
- 89. Two long current carrying thin wires, both with current I, are held by insulating threads of length L and are in equilibrium as shown in the figure, with threads making an angle ' θ ' with the vertical. If wires have mass λ per unit length then the value of I is: $(g = gravitational\ acceleration)$



 $(1) \ 2\sin\theta \sqrt{\frac{\pi\lambda gL}{\mu_0\cos\theta}}$

 $(2) \ 2\sqrt{\frac{\pi g L}{\mu_0} \tan \theta}$

(3) $\sqrt{\frac{\pi \lambda g L}{\mu_0} \tan \theta}$

- (4) $\sin \theta \sqrt{\frac{\pi \lambda g L}{\mu_0 \cos \theta}}$
- 90. On a hot summer night, the refractive index of air is smallest near the ground and increases with height from the ground. When a light beam is directed horizontally, the Huygens' principle leads us to conclude that as it travels, the light beam:
 - (1) goes horizontally without any deflection
- (2) bends downwards

(3) bends upwards

(4) becomes narrower

JEE(MAIN)-2015

ANSWERS

PART A – CHEMISTRY

1.	2	2.	3	3.	1	4.	2
5.	2	6.	4	7.	2	8.	3
9.	1	10.	2	11.	1	12.	1
13.	4	14.	3	15.	1	16.	4
17.	3	18.	3	19.	4	20.	1
21.	3	22.	4	23.	4	24.	4
25.	4	26.	1	27.	4	28.	1
29.	1	30.	3				
		PA	RT B	– MATHEM	IATIC	S	
31.	4	32.	2	33.	3	34.	1
35.	3	36.	2	37.	Corre	ct option is not av	ailable
38.	2	39.	3	40.	3	41.	3
42.	2	43.	3	44.	1	45.	2
46.	3	47.	1	48.	4	49.	4
50.	2	51.	3	52.	4	53.	2
54.	4	55.	3	56.	4	57.	2
58.	3	59.	2	60.	2		
PART C – PHYSICS							
61.	4	62.	1	63.	4	64.	2
65.	2	66.	3	67.	4	68.	1
69.	4	70.	2	71.	4	72.	1
73.	1	74.	2	75.	1	76.	2
77.	2	78.	2, 3	79.	1	80.	2
81.	4	82.	2	83.	2	84.	3
85.	1	86.	2	87.	Corre	ct option is not av	ailable
88.	1	89.	1	90.	3		

HINT AND SOLUTIONS

PART A – CHEMISTRY

1.
$$E_n = -13.6 \times \frac{Z^2}{n^2} \text{ eV}$$
For hydrogen $Z = 1$

$$E_n = -13.6 \times \frac{1}{100} \text{ eV}$$

$$E_n = -13.6 \times \frac{1}{n^2} \text{ eV}$$

$$E_2 = \frac{-13.6}{4} = -3.4 \text{ eV}$$

2.
$$\begin{array}{c} \text{CH}_3 \\ \hline \\ \text{KMnO}_4 \\ \hline \\ \text{(A)} \end{array} \begin{array}{c} \text{COOH} \\ \hline \\ \text{SOCl}_2 \\ \hline \\ \text{(B)} \end{array} \begin{array}{c} \text{CHO} \\ \hline \\ \\ \text{BaSO}_4 \\ \hline \end{array}$$

3.
$$\begin{array}{c} CH_{3} \\ & \downarrow \\ & \downarrow \\ \hline \\ CH_{3} \end{array} \qquad \begin{array}{c} 6 \text{ CH}_{3} \\ \downarrow \\ \hline \\ CH_{3} \end{array} \qquad \begin{array}{c} 6 \text{ CH}_{3} \\ \downarrow \\ \hline \\ CH_{3} \end{array}$$

5 - keto-2 - methyl hexanal

- 4. Ionic radii $N^{3-} > O^{-2} > F^{-}$
- $L \rightarrow M$ charge transfer transition 5.
- 7. Phenelzine is anti-depressant
- $2Al_2O_3 + 3C \longrightarrow 4Al + 3CO_2$ 8.
 - Na₃AlF₆ or CaF₂ is mixed with purified Al₂O₃ to lower the melting point and brings conductivity.
 - Oxygen librated at anode reacts with carbon anode to librate CO and CO₂.
- $TiCl_4 + (C_2H_5)_3Al \rightarrow Ziegler Natta catalyst, used for coordination polymerization.$ 9. $CH_2 = CH_2 \xrightarrow{\text{Wacker process}} CH_3 - CHO + 2HCl$

$$\text{CuCl}_2 \rightarrow \text{used as catalyst in Deacon's process of production of Cl}_2$$
.

 $V_2O_5 \rightarrow$ used as catalyst in Contact Process of manufacturing of H_2SO_4 .

11. Glyptal → Manufacture of paints and lacquers
Polypropene → Manufacture of ropes, toys
Poly vinyl chloride → Manufacture of raincoat, handbags
Bakelite → Making combs and electrical switch

12.
$$\begin{bmatrix} Cl & Py & Cl & NH_3 \\ HOH_2N & NH_3 & HOH_2N & Py & H_3N & NH_2OH \end{bmatrix}^{+}$$

- 13. Higher order (>3) reactions are less probable due to low probability of simultaneous collision of all the reacting species.
- 14. Inter halogen compounds are more reactive than corresponding halogen molecules due to polarity of bond.
- Cu²⁺ + 2e⁻ → Cu
 2F of electricity will give 1 mole of Cu.
- 16. Amount adsorbed = $(0.060 - 0.042) \times 50 \times 10^{-3} \times 60$ = $0.018 \times 50 \times 60 \times 10^{-3}$ = $.018 \times 3$ = .054 gm = 54 mg

Amount adsorbed per gram of activated charcoal = $\frac{54}{3}$ = 18 mg

17.
$$2R-Cl + Hg_2F_2 \xrightarrow{\Delta} 2R-F + Hg_2Cl_2$$

- 18. $2C_8H_7SO_3Na + Ca^{+2} \longrightarrow (C_8H_7SO_3)_2Ca$ 2 mole 1 mole $412 \text{ gm} \qquad 1 \text{ mole}$ Maximum uptake of Ca^{+2} ions by the resin = 1/412 (mole per gm resin)
- 19. Vitamin C is water soluble
- 20. For ion-dipole interaction

 $F \propto \mu \frac{dE}{dr}$ (where μ is dipole moment of dipole and r is distance between ion and dipole)

$$\propto \mu \frac{\mathrm{d}}{\mathrm{dr}} \left(\frac{1}{\mathrm{r}^2} \right)$$

$$\propto \frac{\mu}{r^3}$$

21.
$$\Delta G_{\text{Rex}^{0}}^{\circ} = 2\Delta G_{\text{f}}^{\circ}(\text{NO}_{2}) - 2\Delta G_{\text{f}}^{\circ}(\text{NO}) - \Delta G_{\text{f}}^{\circ}(\text{O}_{2})$$

$$2\Delta G_{\text{f}}^{\circ}(\text{NO}_{2}) = \Delta G_{(\text{Rex}^{n})}^{\circ} + 2\Delta G_{\text{f}}^{\circ}(\text{NO}) + \Delta G_{\text{f}}^{\circ}(\text{O}_{2})$$

$$\Delta G = \Delta G^{\circ} + \text{RT ln } k_{\text{p}}$$
At equilibrium,

$$\Delta G = 0$$
, $Q = k_p$

$$\Delta G^{\circ} = -RT \ln k_{p}$$

$$\Delta G^{\circ}(O_{2}) = 0$$

$$\Delta G_f^0(NO_2) = 0.5[2 \times 86,600 - R(298) \ln(1.6 \times 10^{12})]$$

- 22. $Zn_2[Fe(CN)_6]$ is bluish white and rest are yellow colored compounds.
- 23. Let the organic compound is R Br

$$R - Br + AgNO_3 \longrightarrow AgBr \downarrow$$

So number of moles of AgBr \equiv Number of moles of R - Br \equiv Number of moles of Br

$$\frac{141 \times 10^{-3}}{188}$$
 = number of moles of Br = 0.75 × 10⁻³

Mass of bromine = $0.75 \times 80 \times 10^{-3} \,\text{g} = 60 \,\text{mg}$

Percentage of bromine =
$$\frac{60}{250} \times 100 = 24 \%$$

24. For body center unit cell.

$$4r = a\sqrt{3}$$

So radius of Na =
$$\frac{\sqrt{3} \times 4.29}{4}$$
 = 1.857 \approx 1.86 Å

25. Only 1 phenyl -2-butene can show geometrical isomerism.

$$PhH_2C$$
 H PhH_2C CH_3
 $C=C$ and $C=C$
 H CH_3 H H
 $trans$ cis

Vapour pressure of pure acetone $(p^0) = 185$ torr Vapour pressure of solution (p) = 183 torr Then from Raoult's law,

$$\frac{p^0 - p}{p} = \frac{n_{\text{solute}}}{n_{\text{solvent}}}$$

$$\frac{185 - 183}{183} = \frac{1.2 \, / \, \text{MW}}{100 \, / \, 58}$$

$$\frac{2}{183} = \frac{1.2 \times 58}{100 \times MW}$$

$$MW = \frac{1.2 \times 58 \times 183}{200} = 63.68 \approx 64$$

- 27. H_2O_2 can act both as oxidizing agent as well as reducing agent and H_2O_2 decomposes on exposures to light and dust; so as to kept in plastic or wax lined glass bottles in dark.
- 28. Because of smallest size of Be²⁺, its hydration energy is maximum and is greater than the lattice energy of BeSO₄.

29.
$$\Delta G^0 = -RT \ln K$$

$$2494.2 = -8.314 \times 300 \ln K$$

$$ln K = -1$$

$$\log_{2.718} K = -1$$

$$K = (2.718)^{-1} = \frac{1}{2.718} = 0.3679$$

$$Q_c = \frac{[B][C]}{[A]^2} = \frac{2 \times \frac{1}{2}}{\left(\frac{1}{2}\right)^2} = 4$$

 $Q_c > K_c \Rightarrow$ Reverse direction.

30. The boiling point of Noble gases in increasing order:

Boiling point (K): 4.2< 27.1< 87.2< 119.7< 165< 211

PART B - MATHEMATICS

31.
$$\begin{aligned} t_{r+1} &= {}^{50}C_r \cdot \left(1\right)^{50-r} \cdot \left(-2x^{1/2}\right)^r \\ &= {}^{50}C_r \cdot 2^r \cdot x^{r/2} \left(-1\right)^r \Rightarrow r = \text{even integer.} \\ &\Rightarrow \text{Sum of coefficient} = \sum_{r=0}^{25} {}^{50}C_{2r} \cdot 2^{2r} = \frac{1}{2} \left(\left(1+2\right)^{50} + \left(1-2\right)^{50}\right) = \frac{1}{2} \left(3^{50} + 1\right) \end{aligned}$$

32.
$$\lim_{x \to 0} \left(\frac{x^2 + f(x)}{x^2} \right) = 3, \text{ since limit exits hence } x^2 + f(x) = ax^4 + bx^3 + 3x^2$$

$$\Rightarrow f(x) = ax^4 + bx^3 + 2x^2$$

$$\Rightarrow f'(x) = 4ax^3 + 3bx^2 + 4x$$
also $f'(x) = 0$ at $x = 1, 2$

$$\Rightarrow a = \frac{1}{2}, b = -2$$

$$\Rightarrow f(x) = \frac{x^4}{2} - 2x^3 + 2x^2$$

$$\Rightarrow f(x) = 8 - 16 + 8 = 0.$$

33. New sum
$$\sum y_i = (16 \times 16 - 16) + (3 + 4 + 5) = 252$$

Number of observation = 18
 \Rightarrow New mean
 $\Rightarrow \overline{y} = \frac{252}{18} = 14$.

34.
$$t_{r} = \frac{\sum r^{3}}{\sum (2r-1)} = \frac{r^{2} (r+1)^{2}}{4r^{2}} = \frac{1}{4} (r+1)^{2}$$

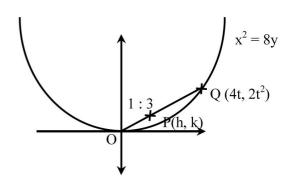
$$S_{9} = \frac{1}{4} \sum_{r=1}^{9} (r+1)^{2}, \text{ let } t = r+1$$

$$= \frac{1}{4} \left(\sum_{t=1}^{10} t^{2} - 1 \right) = 96.$$

35.
$$h = \frac{4t}{4} = t$$

$$k = \frac{2t^2}{4} = \frac{t^2}{2}$$

$$\Rightarrow x^2 = 2y$$



36.
$$x^{2} = 6x + 2 \Rightarrow \alpha^{2} = 6\alpha + 2$$

$$\Rightarrow \alpha^{10} = 6\alpha^{9} + 2\alpha^{8} \qquad ... (1)$$
and $\beta^{10} = 6\beta^{9} + 2\beta^{8} \qquad ... (2)$

$$\Rightarrow \text{Subtract (2) from (1)}$$

$$a_{10} = 6a_{9} + 2a_{8}$$

$$\Rightarrow \frac{a_{10} - 2a_{8}}{2a_{0}} = 3.$$

37. Correct option is not available

Required probability = $\left(\frac{{}^{3}C_{1}{}^{12}C_{3} 2^{9} - {}^{3}C_{2}{}^{12}C_{3}{}^{9}C_{3}}{3^{12}}\right)$

38.
$$\left| \frac{z_{1} - 2z_{2}}{z - z_{1}\overline{z}_{2}} \right| = 1$$

$$(z_{1} - 2z_{2})(\overline{z}_{1} - 2\overline{z}_{2})$$

$$= (2 - z_{1}\overline{z}_{2})(2 - \overline{z}_{1}z_{2})$$

$$\Rightarrow |z_{1}|^{2} - 2z_{2}\overline{z}_{1} - 2\overline{z}_{2}z_{1} + 4|z_{2}|^{2}$$

$$= 4 - 2z_{1}\overline{z}_{2} - 2\overline{z}_{1}z_{2} + |z_{1}|^{2}|z_{2}|^{2}$$

$$\Rightarrow |z_{1}|^{2} + 4|z_{2}|^{2} - 4 - |z_{1}|^{2}|z_{2}|^{2} = 0$$

$$|z_{1}|^{2}(1 - |z_{2}|^{2}) - 4(1 - |z_{2}|^{2}) = 0$$

$$\Rightarrow |z_{1}| = 2 \text{ (as } |z_{2}| \neq 1)$$

39.
$$\int \frac{dx}{x^5 \left(1 + \frac{1}{x^4}\right)^{3/4}}$$

$$1 + \frac{1}{x^4} = t$$

$$\frac{-4}{x^5} dx = dt$$

$$\Rightarrow -\frac{1}{4} \int \frac{1}{t^{3/4}} dt$$

$$= -\frac{1}{4} \times 4t^{1/4} + c = -\left(1 + \frac{1}{x^4}\right)^{1/4} + c.$$

40. x + y < 41, x > 0, y > 0 is bounded region.

> Number of positive integral solutions of the equation x + y + k = 41 will be number of integral co-ordinates in the bounded region.

$$\Rightarrow$$
 ⁴¹⁻¹C₃₋₁ = ⁴⁰C₂ = 780.

Let the point of intersection be $(2 + 3\lambda, 4\lambda - 1, 12\lambda + 2)$ 41.

$$(2+3\lambda)-(4\lambda-1)+12\lambda+2=16$$

$$11\lambda = 11$$

$$\lambda = 1$$

 \Rightarrow point of intersection is (5, 3, 14)

$$\Rightarrow$$
 distance = $\sqrt{(5-1)^2 + 9 + 12^2}$

$$=\sqrt{16+9+144}=13.$$

42. Let equation of plane is $(2x - 5y + z - 3) + \lambda (x + y + 4z - 5) = 0$

As plane is parallel to x + 3y + 6z - 1 = 0

$$\frac{2+\lambda}{1} = \frac{\lambda-5}{3} = \frac{1+4\lambda}{6}$$

$$\Rightarrow$$
 6 + 3 λ = λ - 5

$$11 = -2\lambda$$

$$\lambda = -\frac{11}{2}$$

Also,
$$6\lambda - 30 = 3 + 12\lambda$$

$$-6\lambda = 33$$

$$\lambda = -\frac{11}{2} .$$

so the equation of required plane is

$$(4x - 10y + 2z - 6) - 11(x + y + 4z - 5) = 0$$

$$\Rightarrow$$
 - 7x - 21y - 42z + 49 = 0

$$\Rightarrow$$
 x + 3y + 6z - 7 = 0.

43. The required region

$$= \int_{-\frac{1}{2}}^{1} \left(\frac{y+1}{4} - \frac{y^{2}}{2} \right) dy$$

$$= \frac{1}{4} \left(\frac{y^2}{2} + y \right)_{-\frac{1}{2}}^{1} - \frac{1}{2} \left(\frac{y^3}{3} \right)_{-\frac{1}{2}}^{1}$$

$$=\frac{1}{4}\left(\frac{1}{2}+1-\left(\frac{1}{8}-\frac{1}{2}\right)\right)-\frac{1}{2}\frac{1}{3}\left(1+\frac{1}{8}\right)$$

$$=\frac{1}{4}\times\frac{15}{8}-\frac{3}{16}=\frac{9}{32}$$
.

44. Given

$$1+n=2m$$

$$1, G_1, G_2, G_3, n$$
 are in G.P.

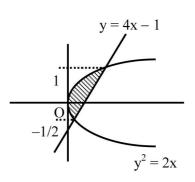
$$1, G_1, G_2, G_3, \Pi$$
 and $\Pi G.1$.

$$\Rightarrow G_1 = \text{lr (let r be the common ratio)}$$

$$G_2 = \text{lr}^2$$

$$G_3 = lr^3$$

$$n = lr^4$$



$$r = \left(\frac{n}{l}\right)^{1/4}$$

$$\Rightarrow G_1^4 + 2G_2^4 + G_3^4 = (lr)^4 + 2 (lr^2)^4 + (lr^3)^4$$

$$= l^4 \times r^4 [1 + 2r^4 + r^8]$$

$$= l^4 \times r^4 [r^4 + 1]^2$$

$$= l^4 \times \frac{n}{l} \left[\frac{n+l}{l}\right]^2$$

$$= ln \times 4m^2$$

$$= 4lnm^2.$$

45. Let M is mid point of BB' and AM is \perp bisector of BB' (where A is the point of intersection given lines)

A is the point of intersection given lines
$$(x-2)(x-1) + (y-2)(y-3) = 0$$

$$\Rightarrow \left(\frac{h+2}{2}-2\right)\left(\frac{h+2}{2}-1\right)+\left(\frac{k+3}{2}-2\right)\left(\frac{k+3}{2}-3\right)=0$$

(-2, 5/3)

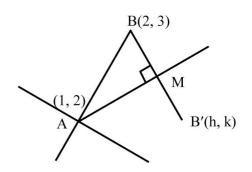
-2, 0)

C

$$\Rightarrow (h-2)(h) + (k-1)(k-3) = 0
\Rightarrow x^2 - 2x + y^2 - 4y + 3 = 0
\Rightarrow (x-1)^2 + (y-2)^2 = 2.$$

$$\Rightarrow$$
 $x^2 - 2x + y^2 - 4y + 3 = 0$

$$\Rightarrow$$
 $(x-1)^2 + (y-2)^2 = 2.$



(2, 5/3)

(a/2, 0)

 $a = 3, b = \sqrt{5}$ 46. $e = \sqrt{1 - \frac{5}{9}} = \frac{2}{3}$

foci =
$$(\pm 2, 0)$$

tangent at P
$$\Rightarrow \frac{2x}{9} + \frac{5y}{3.5} = 1$$

$$\frac{2x}{9} + \frac{y}{3} = 1$$

$$2x + 3y = 9$$

Area of quadrilateral

$$= 4 \times (area of triangle QCR)$$

$$= \left(\frac{1}{2} \times \frac{9}{2} \times 3\right) \times 4 = 27$$

Four digit numbers will start from 6, 7, 8 47. $3 \times 4 \times 3 \times 2 = 72$ Five digit numbers = 5! = 120

48.
$$n(A) = 4, n(B) = 2$$

$$n(A \times B) = 8$$

number of subsets having atleast 3 elements

$$=2^8 - (1 + {}^8C_1 + {}^8C_2) = 219$$

 $\tan^{-1} y = \tan^{-1} x + \tan^{-1} \left(\frac{2x}{1 - x^2} \right)$ 49.

$$= \tan^{-1} \left(\frac{x + \frac{2x}{1 - x^2}}{1 - x \left(\frac{2x}{1 - x^2} \right)} \right)$$

$$= \tan^{-1} \left(\frac{x - x^3 + 2x}{1 - x^2 - 2x^2} \right)$$
$$\tan^{-1} y = \tan^{-1} \left(\frac{3x - x^3}{1 - 3x^2} \right)$$
$$y = \frac{3x - x^3}{1 - 3x^2}.$$

50. Apply the property
$$\int_{a}^{b} f(x) dx = \int_{a}^{b} f(a+b-x) dx$$
And then add

$$2I = \int_{2}^{4} 1 dx$$
$$2I = 2$$

$$I=1$$
.

51.
$$\sim (\sim s \lor (\sim r \land s))$$

$$\equiv s \land (\sim (\sim r \land s))$$

$$\equiv s \land (r \lor \sim s) \equiv (s \land r) \lor (s \land \sim s)$$

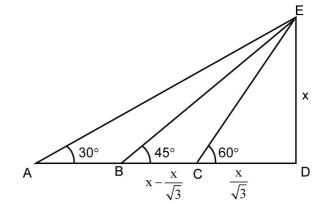
$$\equiv (s \land r) \lor F$$

$$\equiv s \land r.$$

52.
$$AB = \sqrt{3}x - x$$

$$BC = x - \frac{x}{\sqrt{3}}$$

$$\frac{AB}{BC} = \frac{\sqrt{3}x - x}{x - \frac{x}{\sqrt{3}}} = \frac{\sqrt{3}}{1}.$$



53.
$$\lim_{x \to 0} \frac{2\sin^2 x \times (3 + \cos x)}{x \times \left(\frac{\tan 4x}{4x}\right) \times 4x} = \frac{2 \times 4}{4} = 2.$$

54.
$$(\vec{a} \cdot \vec{c}) \vec{b} - (\vec{b} \cdot \vec{c}) \vec{a} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$$

$$\Rightarrow - \vec{b} \cdot \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}|$$

$$\Rightarrow - |\vec{b}| |\vec{c}| \cos \theta = \frac{1}{3} |\vec{b}| |\vec{c}|$$

$$\Rightarrow \cos \theta = -\frac{1}{3}$$

$$\Rightarrow \sin \theta = \frac{2\sqrt{2}}{3} .$$

55.
$$A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{bmatrix}, A^{T} = \begin{bmatrix} 1 & 2 & a \\ 2 & 1 & 2 \\ 2 & -2 & b \end{bmatrix}$$

$$\mathbf{A}\mathbf{A}^{\mathrm{T}} = \left[\mathbf{b}_{ij} \right]_{3 \times 3}$$

$$b_{13} = 0 \Rightarrow 0 = a + 4 + 2b$$

$$b_{23} = 0 \Rightarrow 0 = 2a + 2 - 2b$$

$$\Rightarrow 3a + 6 = 0 \Rightarrow a = -2, b = -1.$$

... (i)

56. for
$$f(x)$$
 to be continuous

$$2k = 3m + 2$$

$$2k - 3m = 2$$

for f(x) to be differentiable

$$\frac{\mathbf{k}}{4} = \mathbf{m}$$

$$k = 4m$$
.

from (i), 8m - 3m = 2

$$5m = 2$$

$$m = \frac{2}{5}$$

$$k = 4 \times \frac{2}{5} = \frac{8}{5}$$

$$k + m = \frac{2}{5} + \frac{8}{5} = \frac{10}{5} = 2.$$

57.
$$(2 - \lambda) x_1 - 2x_2 + x_3 = 0$$

$$2x_1 - (3 + \lambda) x_2 + 2x_3 = 0$$

$$-x_1 + 2x_2 - \lambda x_3 = 0$$

$$\Rightarrow \begin{vmatrix} 2-\lambda & -2 & 1\\ 2 & -3-\lambda & 2\\ -1 & 2 & -\lambda \end{vmatrix} = 0$$

$$(2 - \lambda)(3\lambda + \lambda^2 - 4) + 2(-2\lambda + 2) + 1(4 - 3 - \lambda) = 0$$

$$(2 - \lambda)(\lambda^2 + 3\lambda - 4) + 4(1 - \lambda) + (1 - \lambda) = 0$$

$$(2 - \lambda)((\lambda + 4)(\lambda - 1)) + 5(1 - \lambda) = 0$$

$$(1 - \lambda)((\lambda + 4)(\lambda - 2) + 5) = 0 \Rightarrow \lambda = 1, 1, -3.$$

58.
$$x^2 + 3xy - xy - 3y^2 = 0$$

$$x(x + 3y) - y(x + 3y) = 0$$

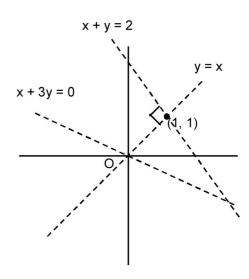
$$(x + 3y)(x - y) = 0$$

Equation of normal is (y-1) = -1(x-1)

$$\Rightarrow$$
 x + y = 2

It intersects x + 3y = 0 at (3, -1)

And hence meets the curve again in the 4th quadrant.



59.
$$C_1(2,3);$$
 $r_1 = \sqrt{4+9+12} = 5$
and $C_2(-3,-9);$ $r_2 = \sqrt{9+81-26} = 8$
 $C_1C_2 = \sqrt{25+144} = 13$
 $C_1C_2 = r_1 + r_2$ touching externally.
 $\Rightarrow 3$ common tangents.

60.
$$\frac{dy}{dx} + \frac{y}{x \ln x} = \frac{2x \ln x}{x \ln x}$$

$$I.F. = e^{\int \frac{1}{x \ln x} dx} = e^{\ln(\ln x)} = \ln x$$

$$y \ln x = \int 2 \ln x dx$$

$$y \ln x = 2 (x \ln x - x) + c$$

$$For x = 1, c = 2$$

$$y \ln x = 2 (x \ln x - x + 1)$$

$$put x = e \Rightarrow y(e) = 2.$$

PART C - PHYSICS

61. As electron goes to ground state, total energy decreases.

$$TE = -KE$$

$$PE = 2TE$$

So, kinetic energy increases but potential energy and total energy decreases.

62.
$$g = \frac{4\pi^2 L}{T^2}$$

$$\frac{\Delta g}{g} = \frac{\Delta L}{L} + 2\left(\frac{\Delta T}{T}\right)$$

$$\frac{\Delta L}{L} = \frac{0.1}{20}, \frac{\Delta T}{T} = \frac{0.01}{0.9}$$

$$100\left(\frac{\Delta g}{g}\right) = 100\left(\frac{\Delta L}{L}\right) + 2 \times 100 \times \left(\frac{\Delta T}{T}\right) \approx 3\%$$

63. It originates from +Ve charge and terminates at -Ve charge. It can not form close loop.

64.
$$f_{R} = f_{C} + f_{m} = 2000 \text{ kHz} + 5\text{kHz} = 2005 \text{ kHz}$$

$$f_{R} = f_{C} - f_{m} = 2000 \text{ kHz} - 5\text{kHz} = 1995 \text{ kHz}$$

So, frequency content of resultant wave will have frequencies 1995 kHz, 2000 kHz and 2005 kHz

65.
$$dQ = dU + dW$$

$$dU = -pdV$$

$$\frac{dU}{dV} = -p = -\frac{1}{3}\frac{U}{V}$$

$$\frac{dU}{U} = -\frac{1}{3}\frac{dV}{V}$$

$$\ell nU = -\frac{1}{3}\ell nV + \ell nC$$

$$U \cdot V^{1/3} = C$$

$$VT^4 \cdot V^{1/3} = C'$$

$$T \propto \frac{1}{R}$$

66. When K_1 is closed and K_2 is open,

$$I_0 = \frac{E}{R}$$

when K_1 is open and K_2 is closed, current as a function of time 't' in L.R. circuit.

$$I = I_0 e^{-R\frac{t}{L}}$$

$$=\frac{1}{10}e^{-5}=\frac{1}{1500}=0.67 \text{ mA}$$

67. Time period,
$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

When additional mass M is added to its bob

$$T_{M}=2\pi\sqrt{\frac{\ell+\Delta\ell}{g}}$$

$$\Delta \ell = \frac{Mg\ell}{AY}$$

$$\Rightarrow T_{M} = 2\pi \sqrt{\frac{\ell + \frac{Mg\ell}{AY}}{g}}$$

$$\left(\frac{T_{\rm M}}{T}\right)^2 = 1 + \frac{Mg}{AY}$$

$$\frac{1}{Y} = \frac{A}{Mg} \left[\left(\frac{T_{M}}{T} \right)^{2} - 1 \right]$$

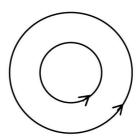
68. Intensity, $I = \frac{1}{2} \epsilon_0 E_0^2 C$, where E_0 is amplitude of the electric field of the light.

$$\frac{P}{4\pi r^2} = \frac{1}{2}\epsilon_0 E_0^2 C$$

$$E_0 = \sqrt{\frac{2P}{4\pi r^2 C\epsilon_0}} = 2.45 \text{ V/m}$$

69. Both solenoid are in equilibrium so, net Force on both solenoids due to other is zero.

So,
$$\vec{F}_1 = \vec{F}_2 = 0$$



70. Average time between collision =
$$\frac{\text{Mean free Path}}{V_{\text{rms}}}$$

$$t = \frac{1}{\frac{\pi d^2 N / V}{\sqrt{\frac{3RT}{M}}}}; \ t = \frac{CV}{\sqrt{T}} \text{ (where } C = \frac{\sqrt{M}}{\pi d^2 N \sqrt{3R}} = \text{constant)}$$

$$\Rightarrow T \propto \frac{V^2}{t^2}$$

For adiabatic

$$TV^{\gamma\text{-}1}=k$$

$$\frac{V^2}{t^2}V^{\gamma-1} = k$$

$$\frac{V^{\gamma+1}}{t^2} = k$$

$$t \propto V^{\frac{\gamma+1}{2}}$$

so,
$$q = \frac{\gamma + 1}{2}$$

71. As
$$L_1 > L_2$$
, therefore $\frac{1}{2}L_1i^2 > \frac{1}{2}L_2i^2$,

 \therefore Rate of energy dissipated through R from L₁ will be slower as compared to L₂.

72.
$$\begin{split} V_{required} &= V_M - V_{M/8} \\ &= -\frac{GM}{2R^3} \left[3R^2 - \frac{R^2}{4} \right] + \frac{GM/8}{2(R/2)^3} \left[3(R/2)^2 \right] \\ &= -\frac{11GM}{8R} + \frac{3GM}{8R} = -\frac{GM}{R} \,. \end{split}$$

73.
$$f_1 \text{ (train approaches)} = 1000 \left(\frac{320}{320 - 20} \right) = 1000 \left(\frac{320}{300} \right) \text{Hz.}$$

$$f_2 \text{ (train recedes)} = 1000 \left(\frac{320}{320 + 20} \right) = 1000 \left(\frac{320}{340} \right) \text{Hz.}$$

$$\Delta f = \left(\frac{f_1 - f_2}{f_1} \right) \times 100\% = \left(1 - \frac{300}{340} \right) \times 100\% = \frac{40}{340} \times 100\%$$

$$= 11.7 \% \approx 12 \%.$$

74. Normal force on block A due to B and between B and wall will be F. Friction on A due to B = 20 N

 \therefore Friction on B due to wall = 100 + 20 = 120 N

75.
$$Z_0 = h - \frac{h}{4} = \frac{3h}{4}$$

76. Since \vec{B} is uniform, only torque acts on a current carrying loop. $\vec{\tau} = (\vec{IA}) \times \vec{B}$ $\vec{A} = A\hat{k}$ for (b) and $\vec{A} = -A\hat{k}$ for (d). $\vec{\tau} = 0$ for both these cases.

The energy of the loop in the \vec{B} field is: $U = -I\vec{A} \cdot \vec{B}$, which is minimum for (b).

77. Taking the potential at Q to be 0 and at P to be V, we apply Kirchoff's current law at Q:

$$\frac{V+6}{3} + \frac{V}{1} + \frac{V-9}{5} = 0$$

$$V = -\frac{3}{23} = -0.13 \text{ volt}$$

The current will flow from Q to P.

78. The potential at the centre = $k \frac{Q}{\frac{4}{3}\pi R^3} \int_0^R \frac{4\pi r^2 dr}{r} = \frac{3}{2} \frac{kQ}{R} = \frac{3}{2} V_0$; $k = \frac{1}{4\pi \epsilon_0}$

$$\therefore$$
 $R_1 = 0$

Potential at surface,
$$V_0 = \frac{kQ}{R}$$

Potential at
$$R_2 = \frac{5V_0}{4} \Rightarrow R_2 = \frac{R}{\sqrt{2}}$$

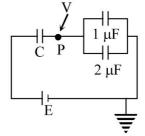
Potential at R₃,
$$\frac{kQ}{R_2} = \frac{3}{4} \frac{kQ}{R} \Rightarrow R_3 = \frac{4R}{3}$$

Similarly at
$$R_4$$
, $\frac{kQ}{R_4} = \frac{kQ}{4R} \Rightarrow R_4 = 4R$

- .. Both options (2) and (3) are correct.
- 79. Let the potential at P be V, Then, C (E–V) = $1 \times V + 2 \times V$ (we take C in μ F)

Or,
$$V = \frac{CE}{3 + C}$$

$$\therefore Q_2 = \frac{2CE}{3+C}$$



80. $E_{initial} = \frac{1}{2}m(2v)^2 + \frac{1}{2}2m(v)^2 = 3mv^2$

$$E_{final} = \frac{1}{2} 3m \left(\frac{4}{9} v^2 + \frac{4}{9} v^2 \right) = \frac{4}{3} m v^2$$

$$\therefore \text{ Fractional loss} = \frac{3 - \frac{4}{3}}{3} = \frac{5}{9} = 56\%$$

81. At face AB,

$$\sin \theta = \mu \sin r$$

At face AC r'
$$< \theta_C$$

$$A-r < \sin^{-1}\frac{1}{u}$$

$$\therefore r > A - \sin^{-1} \frac{1}{\mu}$$

$$\therefore \sin r > \sin \left(A - \sin^{-1} \frac{1}{\mu} \right)$$



$$\begin{split} &\frac{\sin\theta}{\mu} > \sin\left(A - \sin^{-1}\frac{1}{\mu}\right) \\ &\theta > \sin^{-1}\left[\mu\sin\left(A - \sin^{-1}\frac{1}{\mu}\right)\right] \end{split}$$

For maximum possible volume of cube 82.

 $2R = \sqrt{3}a$, a is side of the cube.

Moment of inertia about the required axis = $I = \rho a^3 \frac{a^2}{6}$, where $\rho = \frac{M}{\frac{4}{3}\pi R^3}$

$$I = \frac{3M}{4\pi R^3} \frac{1}{6} \left(\frac{2R}{\sqrt{3}}\right)^5 = \frac{3M}{4\pi R^3} \frac{1}{6} \frac{32R^5}{9\sqrt{3}} = \frac{4MR^2}{9\sqrt{3}\pi} = \frac{4MR^2}{9\sqrt{3}\pi}$$

84.
$$J = ne v_d$$

$$\frac{A\Delta V}{\rho \ell A} = nev_d$$

$$\therefore \quad \rho = \frac{\Delta v}{\ell nev_d} = \frac{5}{0.1 \times 8 \times 10^{28} \times 1.6 \times 10^{-19} \times 2.5 \times 10^{-4}}$$

$$=1.56\times10^{-5}$$

$$\approx 1.6 \times 10^{-5} \,\Omega \text{m}$$

85. At mean position, K.E. is maximum where as P.E. is minimum

86.
$$y_1 = 10t - \frac{1}{2}gt^2$$

$$y_2 = 40t - \frac{1}{2}gt^2$$

$$y_2 - y_1 = 30t$$
 (straight line)

but stone with 10 m/s speed will fall first and the other stone is still in air. Therefore path will become

87. Case (i)
$$\int dS = C \left[\int_{373}^{423} \frac{dT}{T} + \int_{423}^{473} \frac{dT}{T} \right] = ln(473/373)$$

Case (ii) =
$$\int dS = C \left[\int_{373}^{385.5} \frac{dT}{T} + \int_{385.5}^{398} \frac{dT}{T} + \int_{398}^{410.5} \frac{dT}{T} + \int_{410.5}^{423} \frac{dT}{T} + \int_{423}^{435.5} \frac{dT}{T} + \int_{435.5}^{448} \frac{dT}{T} + \int_{448}^{460.5} \frac{dT}{T} + \int_{460.5}^{473} \frac{dT}{T} \right] = ln(473/373)$$

Note: If given temperatures are in Kelvin then answer will be option (1).

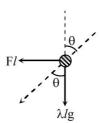
88.
$$\theta = 1.22 \frac{\lambda}{D}$$

Minimum separation = $(25 \times 10^{-2})\theta = 30 \mu m$

89.
$$\tan \theta = \frac{F\ell}{\lambda \ell g} = \frac{\left(\frac{\mu_0 I^2}{4\pi L \sin \theta}\right) \ell}{\lambda \ell g}$$

$$\Rightarrow I = 2 \sin \theta \sqrt{\frac{\pi \lambda L g}{\pi L g}}$$

$$\Rightarrow I = 2\sin\theta \sqrt{\frac{\pi\lambda Lg}{\mu_0\cos\theta}}$$



According to Huygens' principle, each point on wavefront behaves as a point source of light. 90.